# The Relational Model 

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## 1 Administrivia

## Announcements

## Assignment

## From Last Time

Flask tutorial and exercise.

## Outline

1. Relational division
2. Vocabulary
3. Relational model practice

## Coming Up

SQL

## 2 Relational Division

## 3 Vocabulary

1. If $S=\{a, b\}$ and $T=\{1,2,3\}$ then the Cartesian product $S \times T$ has how many ordered pairs? A. 5
B. 6
C. 8
D. 9

Write the ordered pairs.
2. If $S=\{a, b\}$ and $T=\{1,2,3\}$, which of the following can be a relation for $S \times T$ ?
A. $(\mathrm{a}, \mathrm{a}),(\mathrm{a}, \mathrm{b}),(\mathrm{b}, \mathrm{a})$
B. $(\mathrm{a}, 1),(\mathrm{b}, 2)$
C. $(\mathrm{a}, 2),(2, \mathrm{a})$
D. $(\mathrm{a}, 1),(\mathrm{a}, 3),(\mathrm{b}, \mathrm{a})$
3. Each row in a relational table is called a(n)
A. attribute
B. domain
C. relation
D. tuple
4. In the relational model, referential integrity is a constraint that places restrictions on the values of
A. references
B. foreign keys
C. superkeys
D. secondary keys
5. In the relational model, the table in which a foreign key appears as the primary key is called its
A. root relation
B. child relation
C. home relation
D. foreign relation
6. In the relational model, in the SELECT operation, the theta-condition refers to
A. the selection predicate
B. the selection subject
C. the equality or inequality operator used
D. the null condition
7. Which of the following cannot be done using just a PROJECT operator in the relational model
A. eliminating duplicate values
B. operating on more than one column
C. picking out target rows
D. picking out a vertical subset of a table
8. Which of the following operators allows us to combine pieces of information about an entity that appear on separate relational tables?
A. SELECT
B. PROJECT
C. NATURAL JOIN
D. UNION
9. When converting an E-R model to a relational model, the table for a binary relationship can be replaced by a foreign key provided the relationship is not
A. one-to-one
B. one-to-many
C. many-to-one
D. many-to-many
10. In converting from an E-R diagram to a relational model, tables are used to represent
A. entities only
B. relationships only
C. both entities and relationships
D. only entities and attributes
11. If A and B are entity sets with a one-to-one relationship $\mathrm{A}: \mathrm{B}$, all of the following are true of the relational model representation for them EXCEPT
A. the entities A and B may sometimes be combined into a single table with no relationship table needed
B. the relationship should be represented by placing both primary keys as foreign keys in the other table
C. the relationship can be represented by placing the primary key of A as a foreign key in the table for B
D. the relationship can be represented by placing the primary key of B as a foreign key in the table for A

## 4 Relational Model Practice

1. Consider this instance of a Student relation:

| sid | name | login | age | gpa |
| ---: | :--- | :--- | ---: | ---: |
| 50000 | Dave | dave@cs | 19 | 3.3 |
| 53666 | Jones | jones@cs | 18 | 3.4 |
| 53688 | Smith | smith@ee | 18 | 3.2 |
| 53650 | Smith | smith@math | 19 | 3.8 |
| 53831 | Madayan | madayan@music | 11 | 1.8 |
| 53832 | Guldu | guldu@music | 12 | 2.0 |

(a) Give an example of an attribute (or set of attributes) that you can deduce is not a candidate key, based on this instance being legal.
(b) Is there any example of an attribute (or set of attributes) that you can deduce is a candidate key, based on this instance being legal?
2. Consider this relation schema:

Students(sid: string, name: string, login: string,

```
        age: integer, gpa: real)
    Faculty(fid: string, fname: string, sal: real)
    Courses( cid: string, cname: string, credits: integer)
    Rooms(rno: integer, address: string, capacity: integer)
    Enrolled(sid: string, cid: string, grade: string)
    Teaches(fid: string, cid: string)
Meets_In(cid: string, rno: integer, time: string)
```

(a) List all the foreign key constraints among these relations.
(b) Give an example of a (plausible) constraint involving one or more of these relations that is not a primary key or foreign key constraint.
3. Consider the following database instance, which contains information about employees and the projects to which they are assigned:

| Emp |  |  |
| :---: | :---: | :---: |
| empId | 1astName |  |
| E101 | Smith |  |
| E105 | Jones |  |
| E110 | Adams |  |
| E115 | Smith |  |
| Assign |  |  |
| emp Id | projNo | hours |
| E101 | P10 | 200 |
| E101 | P15 | 300 |
| E105 | P10 | 400 |
| E110 | P15 | 700 |
| E110 | P20 | 350 |
| E115 | P10 | 300 |
| E115 | P20 | 400 |


| Proj |  |  |
| :--- | :--- | :--- |
| projNo | projName | budget |
| P10 | Hudson | 500000 |
| P15 | Columbia | 350000 |
| P20 | Wabash | 350000 |
| P23 | Arkansas | 600000 |

Show all the tables (including the intermediate ones) that would be produced by each of the following relational algebra commands:
(a) Symbolically:

$$
\left(\sigma_{\text {lastName='Adams' }}(\mathrm{Emp})\right) \bowtie \text { Assign }
$$

or informally:

```
SELECT Emp WHERE lastName = 'Adams' GIVING T1
T1 JOIN Assign GIVING T2
```

(b) Symbolically:

$$
\Pi_{\text {empId }}\left(\left(\sigma_{\text {budget }>400000}(\operatorname{Proj})\right) \bowtie \text { Assign }\right)
$$

or informally:

```
SELECT Proj WHERE budget > 400000 GIVING T1
T1 JOIN Assign GIVING T2
PROJECT T2 OVER empId GIVING T3
```

4. Using these relations:

Relation S, suppliers entities

| S\# | SNAME | STATUS | CITY |
| :---: | :---: | :---: | :---: |
| S1 | Smith | 20 | London |
| S2 | Jones | 10 | Paris |
| S3 | Blake | 30 | Paris |
| S4 | Clark | 20 | London |
| S5 | Adams | 30 | Athens |

Relation P, parts entities

| P\# | PNAME | COLOR | WEIGHT | CITY |
| :---: | :---: | :---: | :---: | :---: |
| P1 | Nut | Red | 12.0 | London |
| P2 | Bolt | Green | 17.0 | Paris |
| P3 | Screw | Blue | 17.0 | Oslo |
| P4 | Screw | Red | 14.0 | London |
| P5 | Cam | Blue | 12.0 | Paris |
| P6 | Cog | Red | 19.0 | London |

Table SP, suppliers to parts relationship

| S\# | P\# | QTY |
| :--- | :---: | :---: |
| ----- |  |  |
| S1 | P1 | 300 |
| S1 | P2 | 200 |
| S1 | P3 | 400 |
| S1 | P4 | 200 |
| S1 | P5 | 100 |
| S1 | P6 | 100 |
| S2 | P1 | 300 |
| S2 | P2 | 400 |
| S2 | P5 | 420 |
| S3 | P2 | 200 |
| S4 | P2 | 200 |
| S4 | P4 | 300 |
| S4 | P5 | 400 |

Write the sequence of relational algebra commands to find the names of those suppliers that supply all parts weighing 12.0. Remember, division is defined as

$$
\alpha \div \beta=\Pi_{A-B}(\alpha)-\Pi_{A-B}\left(\left(\Pi_{A-B}(\alpha) \times \beta\right)-\alpha\right)
$$

where $A-B$ are those attributes of $\alpha$ not in $\beta$. Before you start writing relational algebra commands to implement the division, you'll need to write commands to construct $\alpha$ and $\beta$.
Show all the tables (including the intermediate ones) that would be produced by each of the relational algebra commands that you write.
5. Consider the following schema for a database that keeps information about business trips and their associated expenses by employees:


Write relational algebra queries for each of the following:
(a) Get a list of all the different destination cities where the employees have taken trips.
(b) Find all the employee information for employees who work in Department 10.
(c) Find the names of all employees who have departed on trips from London.
(d) Find the names of all employees who have any expense item with value 'Entertainment'.
6. Design a relational database schema for the data about the book collector example that you worked on earlier. Start from this E-R diagram:

7. Design a relational database schema for the data about college students, academic advisors, and clubs that you worked on earlier. Start from this E-R diagram:


